

# Evolutionary Computation

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Master Artificial Intelligence

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- The **diversity** measures, in some sense, the **non-similarity** between the individuals of a population.
- E.g., Hamming-distance over the bitstring (using xor):  
 $010010 \otimes 101000 = 111010 \rightarrow 4$
- e.g., delta-distance over the integer (or real) sequence:  
 $\sum_i |x_i - x'_i|$  (being  $x$  and  $x'$  two individuals).
- There are much more **similarity measures**  
<https://link.springer.com/article/10.1186/s40537-025-01227-1> (2025).
- Similar individuals in a population reduce the diversity and the genetic algorithm possibly gets **stuck** in some region of the search space (maybe, but not necessarily, a local minimum).

- To augment the diversity, we have only the mutation operation, provided the mutation becomes visible in the next generation.  
(Observe: whenever an allele disappears in a population, most of the crossover operations cannot regenerate it!)
- Another possibility is just to regenerate a completely or partially **new population**.

We have to draw the decision whether the **best individual(s)** is (are) forced to belong unmodified to the next generation.

- Elitism might help to converge faster.
- Elitism might reduce diversity faster.
- The consequences of this trade-off are problem dependent.

- Add some **aging** to individuals, so even best individuals will eventually be removed from the population.
- Use a **dynamically adapted mutation** rate during the simulation.
- Add a **virus pool** with sequences in the genotype that might be used completely in appropriate operations on certain individuals once in a while.
- Sure there are **more...** (recall: do something, be happy...)

- The **difficulties** of understanding and analyzing genetic algorithms lie in the fact that they implement a combination of random search (by mutation) and biased search (by recombination).
- Genetic algorithms often need unique and problem-specific mutation and recombination operators, which makes it more **challenging** to implement a **generic version** that can be easily applied to different optimization problems.
- **Nature** still has its somewhat better approach: DNA, RNA, gene expression with regulation, proteins, and mitochondria (mtDNA), and, and, and,...  
(e.g. <https://www.ncbi.nlm.nih.gov/books/NBK459456/>)

# evolutionary programming (EP)

Once we have seen GA, **evolutionary programming** is somewhat simpler: it just uses mutation.

- there exist **only** the **phenotypes**, let's say  $x_i$  (for  $i = 1, \dots, n$ ), i.e.,  $n$  individuals in the population
- modification (**mutation**) is realized over the phenotypes as:

$$x'_i = x_i + r_i \sqrt{\beta f(x_i) + \gamma}$$

being  $\beta > 0$  and  $\gamma \geq 0$  tuning parameters (for instance  $\beta = 1$  and  $\gamma = 0$ ) and  $r_i$  is a random value taken from a normal distribution with mean 0 and variance 1 (i.e.,  $r_i \in N[0, 1]^n$ ).

- **Note** that the fitness (objective function  $f$ ) must be shifted, so the minimum is positive.
- Usually a **( $\mu + \mu$ )**-selection strategy is used: all individuals are mutated and the best  $\mu$  individuals are kept.



# EP: principal loop

A evolutionary programming algorithm can be summarized in the following principal loop:

```
InitializePopulation()  
EvaluateIndividuals()  
while not Stopping():  
    GenerateChildrenByMutation()  
    EvaluateIndividuals()  
    ReestablishPopulation()
```

# differential evolution (DE)

Once we have seen GA, **differential evolution** is somewhat simpler: it just uses a special type of recombination (crossover).

- there exist **only** the **phenotypes**, let's say  $x_i$  (for  $i = 1, \dots, n$ ), i.e.,  $n$  individuals in the population
- For each individual, we select **three** other individuals, say  $x_j, x_k, x_l$ , to compute a mutant vector  $v_i$

$$v_i = x_j + F \cdot (x_k - x_l)$$

being  $F \in [0.4, 0.9]$  (usually) a tuning parameter.

- Then we generate an off-spring with a uniform crossover between individual  $x_i$  and mutant  $v_i$  using a certain threshold  $c$
- Usually a  **$(\mu + \mu)$** -like selection strategy is used: all individuals are used to generate off-springs, and the best are kept.

A differential evolution algorithm can be summarized in the following principal loop:

```
InitializePopulation()  
EvaluateIndividuals()  
while not Stopping():  
    GenerateChildrenByDiffusion()  
    EvaluateIndividuals()  
    ReestablishPopulation()
```

## DE: some variations

- One might consider to use always the best individual found so far as individual  $x_j$ .
- The tuning parameter  $F$  might vary, i.e., taking the value from a uniform or a normal distribution.
- One might use DE on discrete sets as well by just rounding the mutants appropriately (or search in the close integer neighborhood according to the dimension of the underlying problem).
- (My opinion) Differential evolution is not just a genetic algorithm, as there is no genotype, rather the other way round: a genetic algorithm using the phenotype as genotype, no mutation, and a random recombination, becomes a differential evolution algorithm.

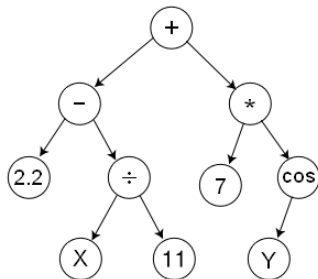
# genetic programming (GP)

Once we have seen GA, **genetic programming** is a genetic algorithm with some special phenotypes and genotypes.

- the genotype is a (simple) program described as a **syntax tree** that can be written as well with **Polish notation** (prefix notation), see next slide...
- the parenthesis can be eliminated, interpretation of the corresponding expression is easy to perform with a **stack automaton**.
- some properties of the execution of the resulting program (as phenotype) are used as fitness (see example, later)

# GP: syntax tree

## syntax tree and Polish notation



$$\left( 2.2 - \left( \frac{X}{11} \right) \right) + \left( 7 * \cos(Y) \right)$$

- $(2.2 - (x/11)) + (7 * \cos(y))$
- $(+ (- (2.2 (/ X 11))) (* (7 \cos(Y))))$
- $+ - 2.2 / X 11 * 7 \cos Y$

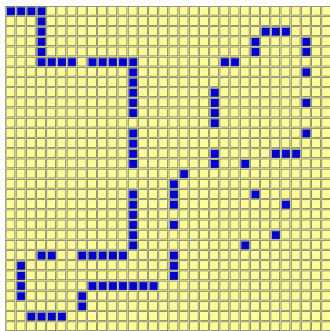
# GP: mutation and crossover operations

- the programs are modified with adequate mutation and crossover operations
- mutation:
  - change a node, but take care to keep a valid syntax tree (maybe subtrees must be removed or added)
  - rotate nodes
  - interchange nodes
- crossover: interchange a subtree of one parent with a subtree of the other parent

# GP: example

Program a robot (ant) that starts at some cell (usually a corner) and tries to find as many objects (food) with as few steps as possible.

Santa Fe Trail



nodes: turn-left, turn-right, move, if-food-ahead

# particle swarm optimization (PSO)

- The inspiration comes from **social behavior of individuals** within an environment including other individuals.
- We work with  $n$  individuals that move in a **continuous**  $d$ -dimensional search space.
- The individuals move (in steps) through the search space and adjust their velocities according to information **gathered from others** (and their own *histories*).
- The individuals are grouped into neighborhoods.

# PSO: velocity actualization

- $x_i$  vector of current positions
- $v_i$  vector of current directional velocities
- $b_i$  best local position vector
- $h_i$  best neighbor position vector
- $\varphi_1, \varphi_2$  influence values (just some *magic*)
- $\xi \in [0.4, 1]$ , e.g.  $\xi = 0.729$  inertia reduction value
- velocity actualization

$$v_i = \xi v_i + U[0, \varphi_1] \circ (b_i - x_i) + U[0, \varphi_2] \circ (h_i - x_i)$$

$$x_i = x_i + v_i$$

- The  $\circ$  operator is either a Hadamard-operation (i.e., component-wise), or a linear operation (i.e., scalar multiplication)

# PSO: principal loop

A particle swarm optimization can be summarized in the following principal loop:

```
InitializePopulation() # i.e.  $x_i$ ,  $v_i$ 
EvaluateIndividuals()  # i.e.  $b_i$ 
DefineNeighborhoodSize()
while not Stopping():
    DetermineNeighborhoodValues() #  $h_i$ 
    UpdateIndividuals()           # i.e.,  $x_i$ ,  $v_i$ ,  $b_i$ 
```

## PSO: some more details

- The velocity can be confined not to pass a certain maximum velocity, which helps to avoid explosion, i.e., that the area of the search space being explored becomes exponentially larger.
- Initial velocities can be zero or some random values.
- Small neighborhoods tend to provide a better global search, while large neighborhoods tend to produce a faster convergence (but maybe premature).
- Neighborhoods can be defined as nearest neighbors, as fixed and overlapping, or entail the entire population, or what-ever-you-like.
- The inertia reduction can be increased with simulation time.
- **Run experiments.**